## Lesson \#3

## Variables, Operators, and Expressions

## Variables

- We already know the three main types of variables in C: int, char, and double. There is also the float type which is similar to double with only single precision. Here we will use double exclusively for floating-point values.
- int is more precise and faster than double.
- A variable, like a memory cell, can only contain one value at a time.
- Putting a value in a variable that contains another value destroys the previous value.


## Variable Declarations

- To reserve space in memory for variables, a declaration statement must be written. A simple declaration consists of the type and the identifier (for example: int $x ;$ ).
- When you declare int $x$; in a C program, the operating system reserves 32 bits at a certain location in the computer's memory to store the variable named $x$.
- The same process applies to char and double variable declarations except that the operating system allocates 8 and 64 bits, respectively.



## Variables and Memory

- Each variable used in C is stored at a specific address in the computer's memory. We do not really care what that address is but it is important for the operating system. The \& operator provides us with the actual address of the variable in memory.
- For example, by declaring int $\mathbf{x}$; I create a variable named $\mathbf{x}$. This variable is stored at the address $\& x$ in the computer's memory.


## Pointer Variables

- We know that the address of $\mathbf{x}$ can be represented by $\boldsymbol{\& x}$. It is possible to put such an address into a variable (known as a pointer variable or simply pointer).
- A pointer is in fact a variable that contains the address of another variable.
- A pointer variable can be int*, char*, or double*, meaning respectively pointer-to-int, pointer-tochar, and pointer-to-double. The type of the pointer must match the type of the variable it points to.


## Pointer Variables

Let's have int $x=10$;
int* ptr ;
$\mathrm{ptr}=\& \mathrm{x}$;

- In the third instruction, we place the address of $x$ into the pointer variable ptr. It is said that ptr points to x .
- The variable ptr, however, must be of a special type ready to hold addresses, specifically addresses of integers (since $x$ is int). So to declare ptr we use the int* type, not int. int* means pointer to integer.


## Pointer Variables

- Note that int* ptr; can also be written int * ptr or int *ptr;.

- The * operator reveals the value of the variable pointed by the pointer variable. Note that the operator can only be applied to a pointer variable. *ptr will follow the arrow to the variable $x$ and reveal its value. So, *ptr is in reality $x$.
- *ptr means: Go to ptr, follow the arrow, get the value.
- printf ("\%d", *ptr); /* will display 10. */


## Inaccuracies

- Putting certain values in a variable can lead to inaccuracies.
- Cancellation error: happens when the magnitude of the operands are too different.
- Ex: 10000.0+0.0000015 would give 10000.0 (This is just an example. In reality the magnitudes must be much more different).
- Arithmetic underflow: happens when a number too small appears as 0 .
- Ex: $0.0000001^{*} 0.0000001$ would give 0.0 (again just an example).


## Inaccuracies

- Arithmetic overflow: happens when the result is too large to be represented. The result is unpredictable. It is quite easy to get an arithmetic overflow using integers.
- Ex: 2000000000+2000000000 (int)


## Arithmetic Operators

- Addition (+): 3+4 or $55.1+43.58$
- Subtraction (-): 50-20 or 45.3-0.78
- Multiplication (*): 5*10 or 0.6*3.4
- Division (/): 50.0/2.0 or 45/2
- Remainder (\%): Also called modulus

Ex: $30 \% 7$ is $2,45 \% 3$ is $0,23 \% 77$ is 23. Important: \% works only with integers!

## Integer Expressions

- Expressions containing only integers are called integer expressions. The result of an integer expression is always an integer. This is particularly important for the division operator.
- For example, $5 / 2$ is an integer division and will give 2, not 2.5.
- There is never a rounding up of values. 99/100 will give 0 not 1.
- Now that we know about integer division, we find that $a \% b$ is the same as $a-\left((a / b){ }^{*} b\right)$.


## Double Expressions

- Expressions containing only doubles are called double expressions. The result of an double expression is always a double.
- For example 5.0/2.0 is a double division and will give 2.5.
-99.0/100.0 will give 0.99.


## Mixed Expressions

- Expressions containing doubles and integers are called mixed expressions. The result of a mixed expression is always a double.
- For example $5 / 2.0$ or $5.0 / 2$ is a mixed division and will give 2.5.
- $35 * 2.0$ will give 70.0.


## Explicit Conversion (Casting)

- The casting (type) operator is used to do explicit conversions when necessary. Let's suppose I want to calculate the average of three integer numbers.
int $\mathrm{a}=4, \mathrm{~b}=3, \mathrm{c}=7$, sum $=0$; /*note the initialization*/ double average; /* need double for average */ sum $=\mathrm{a}+\mathrm{b}+\mathrm{c}$; average $=$ sum $/ 3 ; /^{*} 4.0-$ that is not the correct average! */
- The solution is to convert either the sum or $\underline{3}$ into a double to have a mixed expression.
- average = (double) sum / 3;
- or
- average = sum / 3.0;


## Multiple Operator Expressions

- What if an expression contains multiple operators?

What would be the answer to $3.0+4.0 / 2.0$ ? 3.5 or 5.0 ?

- There must be rules to evaluate expressions; otherwise the result is unpredictable.
- How do you evaluate an expression like $(a+b) / c+a / c-a+b / c * b ?$


## Evaluating Expressions

- Rule \#1: Parentheses rule: All parentheses must be evaluated first from the inside out.
- Rule \#2: Operator precedence rule:
- 2.1 Evaluate unary operators first.
- 2.2 Evaluate *, I, and \% next.
- 2.3 Evaluate + and - next.
- Rule \#3: Associativity rule: All binary operators must be evaluated left to right, unary operators right to left.


## Unary Operators

- Binary operators are the operators with two operands.
- Ex: a+b, b-c, b*a, a\%b, b/c
- Unary operators are the operators with only one operand.
+: the unary plus does nothing (+2 is 2 ).
-     - the unary minus reverses the sign (-(-2)) is 2 , -a reverses the sign of the value of a).


## Unary Operators and Memory

- It is very important to note that the unary minus (-) operator does not affect the value of the variable. Only an assignment operator (or a scanf/fscanf) can change the value.
for example:
$\mathbf{x}=-3$;
printf ("\%्欠", -X) ; /* will display 3 but $x$ is still -3 ! */
$\mathbf{X}=\mathbf{X X} ; /$ now x is $3!$ */


## Expression Building

- Let's have an expression to compute the speed of an object.
- Speed is position2 minus position1 divided by time2 minus time1.
- $\mathrm{s}=(\mathrm{p} 2-\mathrm{p} 1) /(\mathrm{t} 2-\mathrm{t} 1) ;$
- Parentheses can always be used to enhance expression clarity even if they are not necessary.


## Expression Evaluation

Let's evaluate the following expression:
$z-(a+b / 2)+w *-y$

1. The parenthesis is evaluated first: Do b/2 first then add a to the result.
2. The unary operator is evaluated next: -y is evaluated.
3. Next, -y is multiplied by w.
4. Next, $(a+b / 2)$ is subtracted from $z$.
5. Finally, add the result of step \#4 to the result of step \#3.

## Additional Operators

- Some operations cannot be performed with predefined operators. In that case we need special functions.
- A function is a program unit that carries out an operation.
- A function is a "black box" where only what goes in and comes out is known, not its inside mechanisms.



## Square Root

- Square roots in C are computed with a special function taken from a special library: the math library.
- To use that library, we need to include the proper header file: \#include <math.h>
- The square root function is called sqrt and is used by calling it this way: sqrt ( $\mathbf{x}$ ) where x is the number we wish to know the square root of. We can put that answer in another variable $y=\operatorname{sqrt}(x)$;



## Math Functions

- Math functions can be integrated in other C statements and expressions. All math functions use doubles.
- $z=a+\operatorname{sqrt}(b-c) ;$
- printf ("The square root of \%lf is \%lf", x, sqrt(x));


## Other Math Functions

- $y=$ floor ( $x$ ): the largest whole number <= $x$. If $x$ is 3.7, $y$ will be 3.0. If $x$ is -14.2 , $y$ will be -15.0.
- $y=$ ceil $(x)$ : the smallest number $>=x$. If $x$ is 3.7, $y$ will be 4.0. If $x$ is -14.2 , $y$ will be -14.0 .
- $y=\log (x)$ : finds the natural log of $x(\ln )$.
- $y=\log 10(x)$ : finds the decimal log of $x(l o g)$.
- $y=f a b s(x)$ : finds the absolute value of $x$.


## Other Math Functions

- $\sin (x), \cos (x)$, and $\tan (x)$ and are trigonometric functions giving the sine, cosine, and tangent of an angle expressed in radians (not degrees).
- radians = degrees * PI / 180
$y=\exp (x)$ : gives e to the power of $x$. $z=$ pow $(x, y)$ : gives $x$ to the power of $y$. atan(x): calculates the arc tangent of a real number giving an angle expressed in radians.


## Other Functions

- Other functions can be found in the standard library (also need to \#include <stdlib.h>).
- $b=a b s(a)$ : gives the absolute value of an integer.
- $\mathrm{n}=$ rand(): will give a random integer number between 0 and RAND_MAX, a predefined constant macro. To find the value of RAND_MAX on your computer just try this:


## printf ("\%d", RAND_MAX);

## Shortcut Operators

- In some books, you will see some operations in a short form when a variable value is changed by an operation on itself.
- $x=x^{*} 5$; may be shortened to $x^{*}=5$;
- $a=a / 2$; may be shortened to $a /=2$;
- $\mathrm{i}=\mathrm{i}+1$; may be shortened to $\mathrm{i}+=1$;
- Since adding and subtracting 1 is very common, there is a shorter version still.
- i=i+1; may be shortened to ++i;
- i=i-1; may be shortened to - -i;


## Increment and Decrement

- ++i is called an increment; --i a decrement.
- i++ and i-- can also be used.
- There is no difference between the prefix ++i and postfix $i++$ forms as far as the value of $i$ is concerned.
- If an assignment is used, there is a difference. In $\mathrm{b}=++\mathrm{i}$; i is incremented and the answer is then placed into $b$. In $b=i++$, the value of $i$ is placed in $b$ and then $i$ is incremented.
- Note that it is not recommended to use increment and assignment in the same statement.


## End of Lesson

